Vibrationally resolved nitrogen K-shell photoelectron spectra of the dinitrogen oxide molecule: Experiment and theory

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Abstract
Vibrationally resolved N c and N t K-shell photoelectron spectra of the dinitrogen oxide have been studied experimentally and theoretically. Vibrational frequencies for the N c and N t 1s ionized states obtained from the 2D potential surfaces computed by the CCSD(T) method within the equivalent core approximation reasonably agree with the experimental values. Experimental relative intensities of the vibrational structure are reasonably reproduced by the multi-channel Schwinger configuration interaction method (MCSCI) with the computed 2D potential surfaces. Improved relaxed geometries of these core–hole states are obtained from fitting the experimental spectra using the MCSCI calculations and regarding the bond lengths as fitting parameters.

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1. Introduction
Vibrational excitation often accompanies the photoionization of a molecule [1,2]. This is also the case for core-level photoemission [3–5], even though the core electrons are non-bonding and thus a significant change in geometry may not be expected. Reproduction of the vibrational structure observed in the core-level photoelectron spectra has been a challenge to ab initio theory [5–7]. Recent developments of the third generation synchrotron radiation facilities have been providing us with excellent benchmarks for ab initio calculations and the information about the geometry relaxation of the core ionized states [5,9–16].

In the present Letter, we report the experimental and theoretical investigation on the vibrational structure of the N 1s photoelectron spectra of the N 2O molecule. N 2O is a linear molecule that has two nitrogen atoms in different sites, labeled as center (N c) and terminal (N t). We have successfully observed vibrational structures both for the N c and N t core-level photoelectron spectra using monochromatized synchrotron radiation as a light source, as reported elsewhere without details [17]. In the present work, the vibrational spectra are theoretically studied by calculating the two-dimensional (2D) potential energy

[5,8,9]. Indeed vibrationally-resolved core-level photoelectron spectra recorded at the third generation synchrotron radiation facilities have been providing us with excellent benchmarks for ab initio calculations and the information about the geometry relaxation of the core ionized states [5,9–16].
surfaces. The coupled-cluster singles and doubles with non-
iterative triples (CCSD(T)) method is adopted within the
equivalent core approximation (ECA). The ECA has been
frequently used for the analysis and simulation of the vib-
rationally resolved states that appear in the core–hole
states. Simulations based on the ECA often reproduce well
the vibrational spectra providing reliable assignments
[6,18], though a great care is necessary to use the ECA,
because it may cause a significant error in some cases
[18]. Recently, an improved ECA was developed to calcu-
late core–hole states more accurately [19,20]. Relative
intensities for vibrationally resolved photoelectron spectra
are then calculated using the multi-channel Schwinger con-
figuration interaction method (MCSCI) [21–23] within the
adiabatic approximation and using the computed 2D
dependent surfaces. Finally, we extract the equilibrium
governed by the MCSCI and regarding the equilibrium
bond lengths as fitting parameters.

2. Experimental

The measurements were carried out at the c-branch of
the beam line 27SU at SPRing-8, a third generation syn-
chrotron radiation facility with an 8-GeV storage ring in
Japan. The figure-8 undulator installed in this beam line
produces high-intensity linearly polarized soft X-rays.
When integer order (i.e. 1st, 2nd, etc.) harmonics of the
undulator radiation are chosen, the light is horizontally
polarized. The half-integer (i.e. 0.5th, 1.5th, etc.) harmonics
of NO 2 undulator radiation are used. The radiation was
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For a direct comparison between theory and experi-
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The details of these calculations will be given elsewhere
[31]. Briefly, fixed-nuclei photoionization dipole matrix
involves the grid method, in which Lanczos
algorithm was adapted for the diagonalization.

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3. Theoretical

The ground state electronic configuration of the N 2 O
molecule is

\[(1\sigma)^2(2\sigma)^2(3\sigma)^2(4\sigma)^2(5\sigma)^2(6\sigma)^2(1\pi)^4(7\pi)^2(2\pi)^4(1^1\Sigma^+)\].

Here, 1\sigma, 2\sigma and 3\sigma correspond to the O 1s, N c 1s, and N t
1s core orbitals, respectively. The N 2 O molecule has four
vibrational modes, two stretching modes (v^r_1, 0, 0) and
(0, 0, 0, v^r_1) and a doubly-degenerate bending mode (0, v^r_1, 0).
(v^r_1, 0, 0) and (0, 0, v^r_1) are similar to symmetric and anti-
symmetric vibrations, respectively, in CO 2 and thus are
often called quasi-symmetric and quasi-antisymmetric
stretching vibrations. Potential energy surfaces of the
ground, N c 1s core ionized states were calculated for the
two dimensional surfaces along q_1 and q_3, i.e., the
direction of the normal coordinates corresponding to the
quasi-symmetric (v^r_1) and quasi-antisymmetric (v^r_1) stretching
vibrations, in the regions of R^NN = 0.9–1.45 Å and
R^NO = 0.9–1.45 Å. To calculate the 2D potential
energy surface of the core–hole states, the ECA was
adopted. For N c and N t 1s ionized states, the ground states
of NOO \(^+\) and ONO \(^+\), respectively, were calculated using the
CCSD(T) method. The basis sets were correlation
consistent polarized valence triple zeta (cc-pVTZ) basis
sets proposed by Dunning, namely [4s3p2d1f] [29]. The
CCSD(T) calculations were executed with the GAUSSIAN
03 suite of programs [30].

The calculated potential energy surfaces were fitted with
the two dimensional Morse functions [12] and the vibra-
tional analysis was performed. For calculating the spec-
trum, vibrational wave functions and the Franck–Condon
factors were obtained by the grid method, in which Lanczos
algorithm was adapted for the diagonalization.

For a direct comparison between theory and experi-
ment, we have computed vibrationally specific photoioni-
zation cross sections using the MCSCI method [21–23].
The details of these calculations will be given elsewhere
[31]. Briefly, fixed-nuclei photoionization dipole matrix
elements are obtained including two electronic channels
that correspond to ionization leading to the N c and N t hole
states of N 2 O \(^+\). These matrix elements are obtained on a
grid of \{R(NN), R(NO)\} points. The vibrationally specific
matrix elements are then obtained as a 2D integral of the
geometry dependent dipole matrix elements multiplied by
the vibrational wave functions for the ground and ionized
states. Ratios of the cross sections obtained from the result-
ing matrix elements then yield the ratios that can be com-
pared to the experimental data.

4. Results

The N c 1s photoelectron spectrum of N 2 O, in the form of
I(0°) + 2 × I(90°), measured at a photon energy hν = 450 eV, is shown in Fig. 1, together with a least-
squares curve fitting decompositions into a vibrational pro-
gression. Both stretching modes v^r_1 and v^r_2 can in principle
be excited via the N c 1s photoionization. However, it
turned out that one vibrational progression, i.e., quasi-
symmetric stretching mode v^r_1, was enough to fit the spec-
trum of Fig. 1.

The N c 1s photoelectron spectrum of N 2 O, in the form of
I(0°) + 2 × I(90°), measured at a photon energy
$h\nu = 450$ eV, is shown in Fig. 2, together with a least-squares curve fitting decompositions into vibrational progressions. Here, two vibrational progressions, both quasi-symmetric and quasi-antisymmetric modes, $v'_1$ and $v'_3$, were needed to obtain a reasonable curve fit. We assumed that the two modes are uncoupled so that

$$E(v'_1, v'_3) = E(v'_1) + E(v'_3) - E(0, 0).$$

(1)

This difference of the vibrational spectra between $N_c$ 1s and $N_t$ 1s ionizations is related to their characteristic geometry relaxation as discussed later. The spectra in Figs. 1 and 2 were fitted simultaneously, using the PCI-distorted line profiles convoluted with the Gaussian profile. The positions of the first peaks ($v'_1 = v'_3 = 0$) in Figs. 1 and 2, three vibrational frequencies, $\omega_{41}$ for $N_c$ 1s $1s^{-1}$ and $\omega_{40}$ and $\omega_{43}$ for $N_t$ 1s $1s^{-1}$, and the intensities of the individual vibrational components, as well as Lorentzian and Gaussian widths common for all the components, were treated as fitting parameters. The Gaussian width, which represents a convolution of the monochromator bandwidth, electron analyzer bandwidth and Doppler broadening, is $\sim 45$ meV, whereas the Lorentzian width $\Gamma$ is $118 \pm 2$ meV. The extracted vibrational frequencies are summarized Table 1.

The intensity ratios of the vibrational components can be correlated to the ratios of the Franck–Condon factors only if the excitation energy is sufficiently high, i.e., in the sudden limit. As seen in a separate paper [31], the photon energy $450$ eV employed here is not high enough to be completely free from the shape resonance effects. Thus we have computed the ratios obtained from a full photoionization scattering calculation as outlined above using the CCSD(T) potential for the ion states. Both the ratio of $R(v'_1, 0, v'_3)$ results, both the ratios of Franck–Condon factors and the corresponding intensity ratios from the photoionization calculations are given, with the intensity ratio in the parentheses. See the text for details.

Table 1 Vibrational constants, intensity ratios $R(v'_1, 0, v'_3) \equiv I(v'_1, 0, v'_3)/I(0, 0, 0)$ and differences of the equilibrium bond lengths between the neutral and ionic species, $\Delta R_{NN}$ and $\Delta R_{NO}$, for the $N_c$ and $N_t$ 1s ionized states of $N_2O$

<table>
<thead>
<tr>
<th>Exp. (450 eV)</th>
<th>ECA CCSD(T)</th>
<th>ECA CCSD</th>
<th>Opt.</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_c$ 1s $^{-1}$</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma$ (meV)</td>
<td>118(2)</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>$\omega_{41}$ (meV)</td>
<td>136(2)</td>
<td>125</td>
<td>114</td>
</tr>
<tr>
<td>$\omega_{40}$ (meV)</td>
<td>–</td>
<td>225</td>
<td>249</td>
</tr>
<tr>
<td>$\omega_{43}$ (meV)</td>
<td>–</td>
<td>225</td>
<td></td>
</tr>
<tr>
<td>$R(1,0,0)$ (0.60(1))</td>
<td>0.467 (0.472)</td>
<td>0.367</td>
<td>0.592 (0.597)</td>
</tr>
<tr>
<td>$R(2,0,0)$ (0.20(6))</td>
<td>0.110 (0.111)</td>
<td>0.043</td>
<td>0.179 (0.182)</td>
</tr>
<tr>
<td>$R(0,0,1)$ –</td>
<td>–</td>
<td>0.002 (0.004)</td>
<td>0.059</td>
</tr>
<tr>
<td>$R(2,0,1)$ –</td>
<td>–</td>
<td>0.000 (0.002)</td>
<td>0.003</td>
</tr>
<tr>
<td>$\Delta R_{NN}$ –</td>
<td>+0.010</td>
<td>–0.007</td>
<td>+0.012(5)</td>
</tr>
<tr>
<td>$\Delta R_{NO}$ –</td>
<td>+0.043</td>
<td>+0.045</td>
<td>+0.0485(6)</td>
</tr>
<tr>
<td>$\Delta R_{NO}$ –</td>
<td>+0.008</td>
<td>–0.007</td>
<td>–0.0068(9)</td>
</tr>
<tr>
<td>$\Delta R_{NO}$ –</td>
<td>–0.065</td>
<td>–0.071</td>
<td>–0.0661(9)</td>
</tr>
</tbody>
</table>

Theoretical calculations using ECA CCSD(T) and ECA CCSD vibrational potentials are compared with the present experimental values. The results for the optimized geometries (Opt.) are also given. For the theoretical $R(v'_1, 0, v'_3)$ results, both the ratios of Franck–Condon factors and the corresponding intensity ratios from the photoionization calculations are given, with the intensity ratio in the parentheses. See the text for details.
The calculated potential energy surface of the N$_1s$ ionized state, NOO$^+$ in ECA, is metastable and dissociative as NOO$^+ \rightarrow$ NO$^+ + O$. The calculated activation barrier for dissociation is only $\sim$0.80 eV considering the zero point energy correction of 0.155 eV, in which bending modes are also included. In Table 1, we presented the vibrational states up to $\sim$0.35 eV relative to the (000) state. The vibrational spectrum by CCSD(T) reasonably agrees with the experimental spectrum. The vibrational excitations are dominantly due to $v_1$ mode. The vibrational excitations have been underestimated; the calculated vibrational intensity ratios were 0.472 and 0.111 for (100) and (200), respectively, in comparison with the respective experimental values of 0.59 and 0.20. This suggests the underestimate of the geometry change as we discuss later.

For the N$_1s$ ionized state, the theoretical spectrum by CCSD(T) satisfactorily agrees with the experimental spectrum. The vibrational frequencies are calculated to be 175 and 295 meV for $v_1$ and $v_1^*$, respectively, in comparison with the experimental values of 178 and 298 meV. The calculated intensity ratios are 0.819, 0.287, 0.289 and 0.194 for (100), (200), (001) and (101), respectively. These values are in reasonable agreement with the experimental ratios of 0.81, 0.27, 0.33 and 0.21, respectively.

5. Discussion

5.1. Ab initio equilibrium geometries

The geometry change in the core-excited state is of particular interest as outlined in the introduction. The geometry change is sensitive to the level of the theoretical calculations. According to the CCSD(T) calculation of the 2D potential energy surfaces, the equilibrium structures of the ground state and core-ionized states are linear. The optimized bond lengths of the ground state are $R_{NN} = 1.133$ and $R_{NO} = 1.190\ \text{Å}$, which well agree with the experimental values of $R_{NN} = 1.127$ and $R_{NO} = 1.185\ \text{Å}$ [32]. The CCSD(T) calculations indicate that both NN and NO bonds are elongated relative to the ground state, $\Delta R_{NN} = 0.010$ and $\Delta R_{NO} = 0.043\ \text{Å}$, in the N$_c$ 1$s$ ionized state, as listed in Table 1. For the N$_1s$ ionized state, on the other hand, the CCSD(T) calculations predict both NN and NO bonds shrinks, $\Delta R_{NN} = -0.008$, $\Delta R_{NO} = -0.065\ \text{Å}$, as listed in Table 1: the change in $R_{NO}$ is much larger than that in $R_{NN}$.

For comparison, we have carried out the calculations using the CCSD method. The basis set employed is the same as that for CCSD(T), i.e. [4s3p2d1f] [29]. The results are given also in Table 1. As for the ground state geometry (not given in Table 1), the CCSD method gives a very reasonable result. In the N$_c$ 1$s$ ionized state, the CCSD within the ECA predicts that NN bond length is shortened, $\Delta R_{NN} = -0.007$, instead elongated, $\Delta R_{NN} = 0.010$, as predicted by CCSD(T). As a consequence, the results for the intensity ratios of the vibrational components are significantly worse than those predicted by CCSD(T). For the N$_1s$ ionized state, the CCSD calculations predict a geometry change similar to CCSD(T), though the CCSD frequencies are slightly worse than those predicted by CCSD(T). The CCSD results for the vibrational intensity ratios are significantly worse than in the CCSD(T) approximation. We have also examined the basis-set dependence. It turned out that CCSD/cc-pVQZ gives results that are very similar to the CCSD/cc-pVTZ results. These findings illustrate that inclusion of perturbative triple excitations, CCSD(T), is essential for obtaining reasonable agreement with the experimental results.

As pointed out in the introduction, the use of ECA might cause a significant error in certain cases. We thus discuss the restriction stemming from the ECA in the present case. The N$_1s$ ionized state is approximated by the symmetric ONO$^+$ in ECA. As a result, the calculated bond lengths $R_{NN}$ and $R_{NO}$ are identical in ECA. In order to evaluate the accuracy of this restriction, we have carried out direct calculation of the core–hole state, without using ECA, by the SAC-CI method [33,34]. The basis set employed was cc-pCVQZ [4s3p1d] [35]: the use of a larger basis set was difficult given available computational resources. The calculations were executed with the Gaussian 03 suite of programs [36] with some modifications for calculating the core-ionized states in the SAC-CI program, namely, the reference SDT-CI for core–hole states was enabled. The resulting geometry changes are $\Delta R_{NN} = -0.001$ and $\Delta R_{NO} = -0.062\ \text{Å}$, or $R_{NN}$ is slightly longer (0.004 Å) than $R_{NO}$. This direct SAC-CI calculation of the core–hole state, without ECA, suggests that the ECA is approximately valid at least within this accuracy. The vibrational frequencies and vibrational intensity ratios obtained from the SAC-CI 2D potential surfaces (not shown here) are, however, worse than those by CCSD(T) with ECA, indicating that the present SAC-CI calculation with [4s3p1d] is less precise than ECA-CCSD(T) with the larger basis set [4s3p2d1f]. This implies that the SAC-CI results at the present level still suffer from the severe orbital relaxation effect, as discussed in our recent work on C 1$s$ and O 1$s$ ionizations of CO$_2$ [16]. The CCSD(T) with ECA, on the other hand, is free from orbital relaxation effect as a natural consequence of the ECA.

5.2. Obtaining empirical equilibrium geometries

Using the fact that the vibrational intensity ratios are very sensitive to the change of the equilibrium geometries, we have empirically obtained the equilibrium bond lengths of core ionized states, using the theoretical ECA CCSD(T) 2D potential energy surfaces and vibrational wave functions and regarding the equilibrium bond lengths as fitting parameters.

For the N$_c$ 1$s$ ionized state we have only used the experimental branching ratio $R(1,0,0)$ to obtain the equilibrium structure of the ion. Using only one piece of experimental data implies that we can have only one empirical parameter. The optimization was done in this case using the normal modes
of the initial state. We fixed the change in the $\epsilon'_i$ quasi-antisymmetric mode from the ground to the ion state to be that obtained by the CCSD(T) calculations and only treated the change in the $\epsilon'_i$ quasi-symmetric modes as an empirical parameter. The change of the bond lengths found with this empirical optimization, given in Table 1, are $\Delta R_{NN} = +0.0125(3)$ and $\Delta R_{NO} = +0.0048(5)$ Å. The estimated uncertainties in these quantities are obtained using the estimated experimental uncertainty in the $R(1,0,0)$ branching ratio of 0.01. It is worth noting that the change of $R_{NO}$ is much larger than that of $R_{NN}$. We also note that this shift in geometry is close to that found in the CCSD(T) calculation: the optimized values for $\Delta R_{NN}$ and $\Delta R_{NO}$ were slightly larger by 0.002 Å and 0.005 Å, respectively, than the CCSD(T) results. This small change, however, causes a fairly significant change in the $R(1,0,0)$ intensity ratio from 0.472 in the CCSD(T) case to 0.597 in the optimized potential.

For the $N_1$ 1s state, the corresponding optimized potential was obtained fitting the experimental values of $R(1,0,0)$ and $R(0,0,1)$ while adjusting both of the equilibrium bond lengths $R_{NN}$ and $R_{NO}$. The optimized geometry had $\Delta R_{NN} = -0.0068(9)$ Å and $\Delta R_{NO} = -0.0661(9)$ Å with a symmetric geometry to within the experimental uncertainty with $R_{NN} - R_{NO} = 0.0015(18)$ Å. The value of $R_{NN} = R_{NO}$ in the optimized potential is predominantly controlled by the value of $R(0,0,1)$, so that the fairly large uncertainty in $R_{NN} = R_{NO}$ is determined by the experimental uncertainty of 0.02 in $R(0,0,1)$. The value of $R_{NN} + R_{NO}$ in the $N_1$ 1s state is controlled by the value of $R(1,0,0)$ and has the value $R_{NN} + R_{NO} = 2.2395(6)$ Å. It is interesting to note that the terminal $N$ 1s ionization has a larger effect on $R_{NO}$ than on $R_{NN}$.

6. Conclusion

From the $N_c$ and $N_1$ 1s photoelectron spectra of N$_2$O measured at high resolution we have extracted vibrational frequencies and intensity ratios for the $N_c$ and $N_1$ 1s ionized states. Vibrational frequencies obtained from the 2D potential surfaces calculated by the CCSD(T) method within the equivalent core approximation agree well with the experimental values. The vibrational intensity ratios computed by the MCSCI method employing the ab initio 2D potential energy surfaces also agree well with the experimental values. The CCSD gives poorer results, indicating the importance of the inclusion of the perturbative triple, CCSD(T). The validity of the ECA was evaluated with the help of SAC-CI calculation of the core–hole state. The equilibrium geometries of the core–hole states were also determined from the experimental vibrational intensity ratios, using the MCSCI calculations and treating the equilibrium bond lengths as fitting parameters. Knowing these geometries is essential in the ab initio calculations for the photoionization cross sections as will be discussed in detail in a separate letter [31].

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