Potential energy curves of dioxygen anion species, O₂⁻ and O₂²⁻

Hiroshi Nakatsuji and Hiromi Nakai

Department of Synthetic Chemistry, Faculty of Engineering, Kyoto University, Kyoto 606, Japan

Received 20 April 1992; in final form 1 July 1992

The bondings and the potential energy curves of the ground states of the dioxygen anion species, $O_2^-(^2\Pi_g)$ and $O_2^{2-}(^1\Sigma_g^+)$ are studied by the single and double excitation configuration interaction (SD-CI) and the symmetry adapted cluster (SAC)/SAC-CI methods. For O_2^- , the spectroscopic constants calculated by the SD-CI and SAC-CI methods are in reasonable agreement with experiment. For O_2^{2-} , we have found a metastable state in the potential curve, for which the SD-CI calculation gives an equilibrium distance of 1.64 Å and vibrational frequency of 615 cm⁻¹, and the SAC/SAC-CI calculation gives 1.67 Å and 545 cm⁻¹, respectively. The free O_2^- and O_2^{2-} molecules are compared with the superoxide and peroxide species adsorbed on an Ag surface, respectively.

1. Introduction

Dioxygen species play a key role in many important oxidation processes, particularly on conductor and semiconductor surfaces. In surface chemistry, the anion species, superoxide O_2^- and peroxide O_2^{2-} , are more important than the neutral species O_2 , and these anions have been observed by many experimental techniques.

Several electron-spin resonance (ESR) signals due to O₂⁻ have been reported on the surfaces of alkalihalide crystals [1], zeolites [2], ZnO, MgO [3], single crystals of hydrogen peroxide-urea addition compounds [4] and alcohols [5], and Ag [6]. Molecularly adsorbed oxygen has been observed on many metals, particularly on well-defined surfaces such as Cu(100) [7], Cu(110) [7,8], Ag(110) [6,9-15], Ag(111) [16], Pd(100) [17], Pt(110) [18], Pt(111) [13,19,20], and Cr(110) [21]. The O-O stretching vibrational frequency for the adsorbed oxygen has been measured for a few different metal surfaces by several spectroscopic techniques, namely, electron energy-loss spectroscopy (EELS), surfaceenhanced Raman scattering (SERS), etc. The results

Correspondence to: H. Nakatsuji, Department of Synthetic Chemistry, Faculty of Engineering, Kyoto University, Kyoto 606, Japan.

fall into two categories; one with frequencies in the range $740-932 \,\mathrm{cm}^{-1}$ and the other in the range $1075-1195 \,\mathrm{cm}^{-1}$ as mentioned by Jones et al. [22]. The first one was assigned to peroxide species O_2^{2-} , and the second one to superoxide species O_2^{2-} . The frequencies $640 \,\mathrm{cm}^{-1}$ obtained for O_2 on Ag(110) and $660 \,\mathrm{cm}^{-1}$ on Cu(110) were therefore thought to be due to the electron donation from the metal to the oxygen $2p\sigma^*$ orbital. Panas and Siegbahn, on the other hand, have considered from theoretical studies that the ones with frequencies $610-660 \,\mathrm{cm}^{-1}$ are due to peroxide species and those at $870-1020 \,\mathrm{cm}^{-1}$ are due to superoxide species [23].

There are also some observations of the bond length for the chemisorbed O_2 species, mainly by the near edge X-ray absorption fine structure (NEXAFS) method. For example, the bond length of O_2 on Pt(111) is 1.32 ± 0.05 Å, and that of O_2 on Ag(110) is 1.47 ± 0.05 Å [13], which may show the difference between the superoxide and peroxide species.

In the separate papers [24,25] we have investigated the adsorption mechanism of O_2 on an Ag surface by using the dipped adcluster model (DAM) [26,27]. The existence of both molecular superoxide and peroxide species was shown theoretically. For the occurrence of chemisorption, the electron transfer from the bulk metal to the adsorbate and the elec-

trostatic image force between them were shown to be very important. Furthermore, we have shown that the molecular peroxide species, not the superoxide species, is the direct precursor state for the dissociative adsorption of O_2 on a silver surface.

For further understanding the bonding of such adsorbed dioxygen species, it is very important to investigate the electronic structures of the free anion species O_2^- and O_2^{2-} . For O_2 and O_2^- , many experimental works have been reported: for example, Krupenie reviewed the electronic structures and the electronic spectra of O_2 and O_2^- , and gave the potential energy curves of the ground state and some low-lying excited states [28]. On the other hand, no measurements have been made for O_2^{2-} in the gas phase. Though a few theoretical studies are reported for O_2^{2-} [29-32], no studies are reported on the potential energy curve of O22-, and no discussions are made about the comparison between the free anion species O_2^{2-} and the peroxide species observed on a metal surface. In the present letter, we report an ab initio calculation of the potential energy curves of O_2^- and O_2^{2-} and compare them with the dioxygen species on a metal surface, mainly on a silver surface.

2. Gaussian basis set

The purpose of this work is to investigate the electronic structures of the free anion species O_2^- and O_2^{2-} and to compare them with the dioxygen species, superoxide and perodixe, on a silver surface. We therefore use the same basis set as that used for the studies of O_2 adsorbed on a silver surface [24,25]; namely, the Huzinaga-Dunning [4s2p] set [33] augmented by the diffuse s, p functions of $\alpha = 0.059$ [34] and the polarization d function of $\alpha = 0.30$.

We first examine the electron affinity (EA) of the oxygen atom. The EA calculated by the delta-self-consistent-field (Δ SCF) procedure is a negative value of -0.52 eV, and does not explain the experimental value of 1.46 eV even in sign. On the other hand, the result of the single and double excitation configuration interaction (SD-CI) method is a positive value of 0.97 eV, which shows that electron correlation is essential for calculating the EA of the oxygen atom. However, the agreement with the experimental value is not particularly good in comparison with the pre-

vious works [35-41]. For obtaining further agreement, it is necessary to use larger basis sets and a larger expansion of the configuration space. For ex-Sasaki and Yoshimine used (8s7p6d5f4g3h2i) Slater type basis set and obtained an EA of 1.04 eV by the SD-CI calculations. Feller and Davidson used the (23s12p10d5f3g) uncontracted basis set containing a total of 171 functions. and adopted more than 200000 and 300000 configurations for the neutral and anion atoms, respectively, in the multi-reference (MR) SD-CI calculations. The calculated EA was 1.31 eV, which differs from the experimental value by only 0.15 eV.

3. Potential energy curves of dioxygen anion species

The electronic structures and the potential energy curves of the ground states of the dioxygen species $O_2(^3\Sigma_g^-)$, $O_2^-(^2\Pi_g)$, and $O_2^{2-}(^1\Sigma_g^+)$ are calculated by the restricted Hartree–Fock (HF) and the SD-CI methods. Furthermore, symmetry adapted cluster (SAC)/SAC-CI calculations [42,43] are performed for the anion species O_2^- and O_2^{2-} , and the calculated potential energy curves are shown in fig. 1.

The $1\sigma_g\,,\ 1\sigma_u,\ 2\sigma_g$ and $2\sigma_u$ molecular orbitals

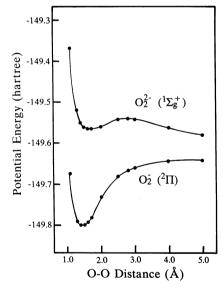


Fig. 1. Potential energy curves of the ground state of the dioxygen anion species, ${\rm O}_2^-$ and ${\rm O}_2^{2-}$ calculated by the SAC/SAC-CI method.

(MOs), which correspond to the 1s and 2s atomic orbitals (AOs), are frozen in the CI and SAC/SAC-CI calculations, and five higher occupied orbitals are used in the active space. In the previous studies for the oxygen adsorption onto an Ag surface [24,25], the 1s and 2s AOs of oxygen were also treated as frozen core orbitals. Since the energies of the highest four unoccupied orbitals, which are mainly composed of the s AOs, are higher than 3.5 hartree and almost constant at all the separations, they are also frozen in the present calculations.

No configuration selections for the linked operators are made in the SAC/SAC-CI calculations. In the SAC calculations of O_2^{2-} , all single and double excitation operators are used as the linked operators, and therefore the dimension of the SAC Hamiltonian matrix is equal to that of the SD-CI matrix. In the SAC-CI calculations of the O_2^{-} species, it is expressed as the ionized state of the dianion species. Because of the merit of the SAC/SAC-CI theory, the dimension of the linked terms in the SAC-CI calculation is notably small compared with the usual CI method: namely, 82 and 1234 in the SAC-CI and SD-CI calculations, respectively. The HF and CI calculations are carried out by the GAMESS program

[44], and the SAC/SAC-CI calculations by the SAC85 program [45].

Table 1 shows the equilibrium distance, the vibrational frequency, and the dissociation energy of the dioxygen species. The quantities calculated for the superoxide and peroxide on an Ag surface [24] are also shown for comparison. These spectroscopic constants are calculated by analytically fitting the present theoretical curve to the extended Morse function [46], and the vibrational energy levels are given by [47]

$$E_{v} = \omega_{e}(v + \frac{1}{2}) - \omega_{e} x_{e}(v + \frac{1}{2})^{2} + \omega_{e} y_{e}(v + \frac{1}{2})^{3} + \omega_{e} z_{e}(v + \frac{1}{2})^{4}.$$
(1)

Since O_2 and O_2^- have unpaired spins in the $1\pi_g$ orbitals, they have permanent magnetic moments. The bond order of the dioxygen species decreases as the occupation of the $1\pi_g$ orbital increases, and therefore the bond lengths are calculated to be longer and the vibrational frequencies to be smaller as the $1\pi_g$ occupation increases.

The bond lengths of O_2 and O_2^- calculated by the HF method are closer to the experimental values than those calculated by the SD-CI method. A reason

Table 1
The bond lengths R_e , vibrational frequencies ω_e , dissociation energies D_e , electron affinities EA, and gross charges of the O_2 , O_2^- , and O_2^{2-} molecules in the gas phase and the superoxide O_2^{2-} and peroxide O_2^{2-} species on a silver surface

Species	Method	R _e (Å)	$\omega_{ m e}$ (cm ⁻¹)	D _e (eV)	EA (eV)	Gross charge (per O ₂)
$\overline{\mathrm{O_2}}$	HF	1.20	1856	16.64	-0.06	0
	SD-CI	1.27	1445	7.25	0.52	0
	exp.	1.21	1580	5.12	0.44	0
O_2^-	HF	1.33	1420	10.61	-7.76	-1
	SD-CI	1.42	1078	5.38	-6.68	-1
	SAC-CI	1.44	1010	4.00	-6.24	-1
	exp.	1.35	1090	4.09		-1
O_2^{2-}	HF	1.53	836	2.91		-2
	SD-CI	1.64	615	$-2.21 (1.14)^{b}$		-2
	SAC	1.67	545	$-2.94(0.703)^{b}$		-2
O ₂ on Ag ^{a)}	SAC-CI	1.47	974, 1055			-0.54, -0.65
-	exp.		1053			·
O ₂ ²⁻ on Ag ^{a)}	SAC-CI	1.66	689			-1.4
_	exp.	1.47 ± 0.05	628-697			

a) Ref. [24].

b) Values in parentheses are the hump heights.

would be a lack of harder polarization d functions, which are expected to shorten the O-O length. On the other hand, the overestimation of the vibrational frequencies by the HF method is improved by including electron correlations.

In the previous study of the adsorbed oxygen species on an Ag surface [24], we used the SAC/SAC-CI method. The existence of the two superoxide species was shown for the side-on form; one has an unpaired electron in the π^* orbital parallel to the surface and the other in the perpendicular π^* orbital. The calculated bond lengths are 1.47 Å together and the vibrational frequencies are 1055 and 974 cm⁻¹, respectively. These values are similar to those of the free O₂ molecule calculated by the SAC-CI method, suggesting that the bonding in the molecular superoxide species absorbed on an Ag surface is similar to that of the free O₂ molecule. The cross charges of the superoxide species are -0.54 and -0.65, respectively, in contrast to -1.0 for a free molecule, by the back-donation from O₂ to an Ag surface.

The EA of O_2 is also shown in table 1. While the EA calculated by the Δ SCF procedure is negative as for the oxygen atom, that calculated by the SD-CI method is properly positive. The discrepancy from the experimental value is +0.12 eV, which is comparatively small. The previous study [48] using the Møller-Plesset (MP) perturbation method gave an EA of -1.03 to +1.15 eV with several Gaussian basis sets.

At the dissociation limit, O_2 and O_2^- become $O(^3P) + O(^3P)$ and $O(^3P) + O^-(^2P)$, respectively, and the energy difference between them corresponds to the EA of an oxygen atom. The SD-CI calculations give a difference of 2.43 eV in comparison with the experimental value of 1.46 eV, and the disagreement of +0.97 eV is very large. The dissociation energies of O_2 and O_2^- are calculated to be larger than the experimental values by +2.08 and +1.29 eV, respectively. These large disagreements are due to the truncated and size-inconsistent nature of the CI method. On the other hand, the dissociation energy of O_2^- is calculated to be 4.00 eV by the SAC-CI method. The discrepancy from the experimental value is +0.09 eV, which is very small.

The anharmonicity terms $\omega_e x_e$, $\omega_e y_e$, and $\omega_e z_e$ of O_2^- estimated from the SAC-CI calculations are 7.31, 3.01×10^{-3} , and 1.25×10^{-4} cm⁻¹, respectively,

while the experimental value of $\omega_e x_e$ is 11.7 ± 4 cm⁻¹ [28]. From eq. (1), 47 vibrational levels (v=0–46) are obtained for the bound state of O_2^- , of which the lowest 16 and the highest 10 levels are shown in table 2. The level spacing between v=0 and 1 is 995 cm⁻¹, which is not equal to the vibrational frequency shown in table 1, because of the anharmonicity of the curve: see eq. (1).

Different from O_2 and O_2^- , the O_2^{2-} molecule has no unpaired spins and, therefore, no permanent magnetic moments. While O_2^{2-} is a closed-shell molecule, it shows a Hartree-Fock instability at longer bond length: namely, the unrestricted HF solution is lower than the restricted HF one. The potential energy curve calculated by the HF method does not have a hump due to the electrostatic interaction between the two negative oxygen atoms. On the other hand, the potential energy curves calculated by the SD-CI and SAC methods have humps around the O-O distance of 2.8 Å. The metastable state around the O-O distance of 1.6 Å is based on the $3\sigma_a$ bond. By fitting the present curve to the extended Morse function at the region shorter than the O-O distance of 2.8 Å, the length is calculated to be 1.64 and 1.67 Å by the SD-CI and SAC methods, respectively, and the O-O vibrational frequency to be 615 and 545 cm⁻¹, respectively. The anharmonicity terms $\omega_{\rm e}x_{\rm e}$, $\omega_{\rm e} y_{\rm e}$, and $\omega_{\rm e} z_{\rm e}$ of ${\rm O_2^{2-}}$ estimated by the SAC calculation are 10.9, 6.48×10^{-3} , and -2.99×10^{-4} cm⁻¹, respectively. The hump height from the potential minimum at the O-O distance of 1.67 Å is calculated to be 0.703 eV (5670 cm⁻¹) by the SAC method. For the metastable state of O_2^{2-} , we obtain 15 vibrational levels (v=0-14), and the results are shown in table 2.

The calculated bond length of the peroxide species on an Ag surface is similar to that for the free O_2^{2-} molecule, though the experimental value is 1.47 ± 0.05 Å. The vibrational frequency, on the other hand, is different: that of the free molecule is smaller than that on a silver surface. This is in accordance with the fact that O_2^{2-} is stable on the surface, but only metastable in the gas phase. The gross charge of the peroxide species on the surface is -1.4 by the backdonation from O_2 to the Ag surface, in contrast to 2.0 in the gas phase.

At the region longer than the O-O distance of 2.8 Å, the potential energy curve of O_2^{2-} is repulsive due

Table 2 Vibrational levels of the ground states of O_2^- and O_2^{2-}

Vibrational level	O_2^-		O_2^2		
v	wave number E_{ν} (cm ⁻¹)	level spacing $E_{\nu} - E_{\nu-1}$ (cm ⁻¹)	wave number E_v (cm ⁻¹)	level spacing	
	D_{v} (cm.)			$E_{\nu} - E_{\nu-1} \; (\text{cm}^{-1}$	
0	503		270		
1	1498	995	793	523	
2	2479	981	1295	502	
3	3444	965	1774	479	
4	4396	952	2233	459	
5	5333	937	2669	436	
6	6255	922	3084	415	
7	7163	908	3477	393	
8	8057	894	3849	372	
9	8936	879	4199	350	
10	9801	865	4527	328	
11	10651	850	4833	306	
12	11488	837	5118	285	
13	12310	822	5381	263	
14	13118	808	5622	241	
15	13912	794			
37	27991	507			
38	28486	495			
39	28969	483			
40	29440	471			
41	29900	460			
42	30349	449			
43	30787	438			
44	31213	426			
45	31629	416			
46	32034	405			

to the interaction between negatively charged atoms as mentioned above. Fig. 2 shows the potential energy curve plotted against the reciprocal of the O-O distance in au. The points in the figure correspond to O-O distances of 2.8, 3.0, 4.0, 5.0, and 10.0 Å, respectively. This figure shows that the slope of the curve asymptotically approaches unity as the distance is elongated, which means that the interaction is due only to the electrostatic repulsion. The energy at the dissociation limit, which is used for calculating the dissociation energy of O_2^{2-} as shown in table 1, is estimated by subtracting the electrostatic energy from the potential energy. The difference between the energies of O_2^- and O_2^{2-} at the dissociation limit, which corresponds to the EA of the oxygen atom as mentioned before, is calculated to be 0.82 eV. This value is closer to and a little smaller than the EA of the oxygen atom calculated in the present study, i.e. 0.97 eV. A reason of this underestimation is that the 2s orbital is frozen in the molecular calculations, while it was not in the atomic calculations.

The O_2^{2-} molecule is less stable than the O_2^{-} molecule by 6.19 eV, and does not exist, as a stable species, in the gas phase. This calculated valence state of O_2^{2-} , which is an electron-attached state of O_2^{-} , is embedded in the continuum of the O_2^{-} . On the Ag surface, on the other hand, the peroxide O_2^{2-} species is more stable than the superoxide O_2^{-} species. The main difference of the metal surface from the gas phase is that the O_2^{2-} species is stabilized by the dangling bonds of the surface atoms and by the electrostatic image force. The image force stabilizes both

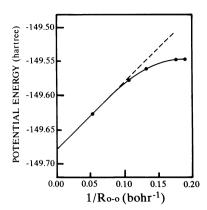


Fig. 2. Potential energy curves of the ground state of O_2^{2-} calculated by the SAC method. The horizontal axis shows the reciprocal of the O-O distance in au. The dashed line with the slope of unity means that the electrostatic repulsion is a main interaction between negatively charged oxygen atoms.

 ${\rm O}_2^-$ and ${\rm O}_2^{2-}$ species, but the stabilization of ${\rm O}_2^{2-}$ is larger than that of ${\rm O}_2^-$. Therefore, the adsorption energy calculated for the peroxide species on an Ag surface is larger than that for the superoxide species [24]. The image force does not affect the geometries of the adsorbed species much because it is a longrange force in comparison with the force for chemical bonding. Further, the potential curves of dioxygen species shown in fig. 1 correspond well with the fact that the molecular peroxide species, not the superoxide species, is the direct precursor state for the dissociatively adsorbed oxygens on an Ag surface [24].

4. Concluding remarks

In the present Letter, we have theoretically studied the electronic structures of the ground state of the free dioxygen species $O_2(^3\Sigma_g^-)$, $O_2^-(^2\Pi)$, and $O_2^{2-}(^1\Sigma_g^+)$. We first examine the electron affinity (EA) of the oxygen atom, in which all of the diffuse s, p and polarization d functions are necessary for describing the EA. A reasonable value for the EA is obtained only after including electron correlations; the EA of O calculated by the Δ SCF procedure does not agree with the experimental value even in sign.

For O_2^- , the spectroscopic constants calculated by

the SAC-CI method agree well with the experiments. In the potential curves of O_2^{2-} obtained by the SD-CI and the SAC calculations, there is a metastable state which reflects the $3\sigma_g$ bond. The equilibrium distance of this state is calculated to be 1.64 and 1.67 Å and the vibrational frequency to be 615 and 545 cm⁻¹ by the SD-CI and SAC methods, respectively.

The bonding of the free O_2^- molecule is similar to that of the molecular superoxide species on a silver surface. However, the bonding of the O_2^{2-} in the gas phase is somewhat different from that of the peroxide species on the surface. The stabilities of the superoxide and peroxide species on the surface are opposite to those of the free O_2^- and O_2^{2-} molecules, because of the effects of the dangling bonds and the image force on the surface. O_2^{2-} receives a larger image force than O_2^- on the surface. We note that the image force is a long-range force, in comparison with the force for chemical bonding, so that it does not affect the geometries and vibrational frequencies of the adsorbed species much, but affects the adsorption energy and stability more.

We expect that the knowledge of the electronic structures and potential energy curves of the free dioxygen species as shown in the present study gives insight for studying the dioxygen species adsorbed on metal surfaces.

Acknowledgement

The calculations have been carried out with the computers at the Data Processing Center of the Kyoto University and at the Institute for Molecular Science. Part of this study was supported by the Grantin-Aid for Scientific Research from the Ministry of Education, Science, and Culture of Japan.

References

- [1] W. Känzig and M.H. Cohen, Phys. Rev. Letters 3 (1959) 509.
- [2] P.H. Kasai, J. Chem. Phys. 43 (1965) 3322.
- [3] J.H. Lunsford and J.P. Jayne, J. Chem. Phys. 44 (1966) 1487.
- [4] T. Ichikawa, M. Iwasaki and K. Kuwata, J. Chem. Phys. 44 (1966) 2927.

- [5] G.W. Eastland and M.C.R. Symons, J. Phys. Chem. 81 (1977) 1502.
- [6] R.B. Clarkson and S. McClellan, J. Phys. Chem. 82 (1978) 294.
- [7] A. Spitzer and H. Lüth, Surface Sci. 118 (1982) 121.
- [8] K. Prabhakaran, P. Sen and C.N.R. Rao, Surface Sci. 177 (1986) L971.
- [9] M.A. Bartreau and J. Madix, Surface Sci. 97 (1980) 101.
- [10] B.A. Sexton and R.J. Madix, Chem. Phys. Letters 76 (1980)
- [11] C. Backx, C.P.M. deGroot and P. Biloen, Surface Sci. 104 (1981) 300; Appl. Surface Sci. 6 (1980) 256.
- [12] K. Bange, T.E. Madey and J.K. Sass 113 (1985) 56.
- [13] D.A. Outka, J. Stöhr, W. Jark, J. Solomon and R.J. Madix, Phys. Rev. B 35 (1987) 419.
- [14] J. Stöhr and D.A. Outka, Phys. Rev. B 36 (1987) 7891.
- [15] K.C. Prince, G. Paolucci and A.M. Bradshaw, Surface Sci. 175 (1986) 101.
- [16] C.T. Campbell, Surface Sci. 157 (1985) 43.
- [17] C. Nyberg and C.G. Tengstål, Surface Sci. 126 (1983) 163.
- [18] K. Prince, K. Duckers, K. Horn and V. Chab, Surface Sci. 200 (1988) L451.
- [19] J.L. Gland, B.A. Sexton and G.B. Fisher, Surface Sci. 95 (1980) 587.
- [20] W. Eberhardt, T. Upton, S. Cramm and L. Inococcia, Chem. Phys. Letters 146 (1988) 561.
- [21] N.D. Shinn and T.E. Madey, Surface Sci. 176 (1986) 635.
- [22] R.D. Jones, D.A. Summerville and F. Basolo, Chem. Rev. 79 (1979) 13.
- [23] I. Panas and P. Siegbahn, Chem. Phys. Letters 153 (1988) 458.
- [24] H. Nakatsuji and H. Nakai, Chem. Phys. Letters 174 (1990) 283; J. Chem. Phys., submitted for publication.
- [25] H. Nakatsuji and H. Nakai, Can. J. Chem., in press.
- [26] H. Nakatsuji, J. Chem. Phys. 87 (1987) 5759.
- [27] H. Nakatsuji, H. Nakai and Y. Fukunishi, J. Chem. Phys. 95 (1991) 640.
- [28] P.H. Krupenie, J. Phys. Chem. Ref. Data 1 (1972) 423.
- [29] G. Chambaud, B. Levy and P. Millie, Theoret. Chim. Acta 48 (1978) 103.

- [30] A.H. Pakiari and J.W. Linnett, Intern. J. Quantum Chem. 18 (1980) 661.
- [31] G. Leroy, D. Peeters and M. Thange, J. Mol. Struct. 123 (1985) 243.
- [32] M. Roch and J. Weber, Chem. Phys. Letters 115 (1985) 268.
- [33] S. Huzinaga, J. Chem. Phys. 42 (1965) 1293;T.H. Dunning Jr., J. Chem. Phys. 53 (1970) 2823.
- [34] T.H. Dunning Jr. and P.J. Hay, Modern theoretical chemistry, Vol. 3, ed. H.F. Schaefer III (Plenum Press, New York, 1977).
- [35] B.H. Botch and T.H. Dunning Jr., J. Chem. Phys. 76 (1982) 6046.
- [36] F. Sasaki and M. Yoshimine, Phys. Rev. A 9 (1974) 17, 26.
- [37] D. Feller and E.R. Davidson, J. Chem. Phys. 82 (1985) 4135; 90 (1988) 1024.
- [38] K. Raghavachari, J. Chem. Phys. 82 (1985) 4142.
- [39] C.W. Bauschlicher Jr., S.R. Langhoff, H. Partridge and P.R. Taylor, J. Chem. Phys. 85 (1986) 3407.
- [40] J.A. Pople, P. von R. Schleyer, J. Kaneti and G.W. Spitznagel, Chem. Phys Letters 145 (1988) 359.
- [41] T. Noro, M. Yoshimine, M. Sekiya and F. Sasaki, Phys. Rev. Letters 66 (1974) 1157.
- [42] H. Nakatsuji and K. Hirao, J. Chem. Phys. 68 (1978) 2035.
- [43] H. Nakatsuji, Chem. Phys. Letters 59 (1978) 362; 67 (1979) 329, 334.
- [44] B.R. Brooks, P. Saxe, W.D. Laidig and M. Dupuis, Program System GAMESS; Program Library No. 481, Computer Center of the Institute for Molecular Science (1981).
- [45] H. Nakatsuji, Program System for SAC and SAC-CI calculations, Program Library No. 146 (Y4/SAC), Data Processing Center of Kyoto University (1985); Program Library SAC85, No. 1396, Computer Center of the Institute for Molecular Science (1981).
- [46] H.M. Hulburt and J.O. Hirschfelder, J. Chem. Phys. 9 (1941) 61; 35 (1961) 1901.
- [47] J.L. Dunham, Phys. Rev. 41 (1932) 713, 721.
- [48] J.J. Novoa and F. Mota, Chem. Phys. Letters 135 (1985)